

### **Aircraft Design**

#### Lecture 2: Aerodynamics

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### Introduction

- Aerodynamics is the study of the loads exerted by the flow of air over an aircraft (there are other applications but they are boring)
- There are six loads:
  - Three forces:
    - Lift
    - Drag
    - Sideforce
  - Three moments:
    - Pitch
    - Roll
    - Yaw





## Why study aerodynamics?

- Anything can fly, as long as you put a big enough rocket engine under it. But:
  - That's the most expensive and dangerous solution
  - There are still stability, control and other problems that can only be resolved through a good aerodynamic study
  - There are several much better solutions. A few of them are listed in the next couple of slides. They all require a good understanding of aerodynamics.





#### Air vehicles

- Airship
  - A hydrostatic force provides lift
  - Motor(s) provide forward acceleration
- Airplane
  - A lifting surface (wing) provides lift
  - Motor(s) provide forward acceleration
- Helicopter
  - A rotor provides lift
  - The same rotor rotor provides forward acceleration
- Autogyro
  - A rotor provides lift
  - Another rotor provides forward acceleration







#### More air vehicles

- Glider
  - A lifting surface (wing) provides lift
  - There is no forward acceleration
- Missile
  - Several small lifting surfaces provide lift
  - A motor provides forward acceleration
- Hot air balloon
  - A hydrostatic force provides lift
  - There is no forward acceleration
- Lifting body
  - A lifting body provides lift
  - A motor provides forward acceleration (optional)











#### Airplane

- In this course we will mostly talk about airplanes
- The most popular airplane configuration is wing+fuselage+tail
- The configuration mirrors birds. The Wright brothers and others before them were inspired by bird flight
- Each component has a distinct role:
  - The wing provides lift
  - The fuselage holds cargo, passengers etc
  - The tail provides stability and control



## Wings

- The role of the wing is to generate lift
- Lift creation can be described in two ways:
  - Pressure differential: The air pressure on the bottom surface of the wing is higher than the air pressure of the top surface. This pressure difference creates a net force upwards
  - Newton's third law: The wing pushes air downwards. As a consequence, the air itself pushes the wing upwards.
  - Either way, the laws of conservation apply: mass, momentum and energy.



#### Lift generation

- Lift generation of wings depends on their cross-sectional shape
- The Wright brothers were the first to study the effects of different cross sectional shape
- They determined that the airfoil is the optimum cross-sectional shape for a wing



### Airfoils

#### Flow visualization

#### Flow over aerofoils

#### **H** Babinsky



Cambridge University Department of Engineering Pulsed jets show that the flow moves faster over the top surface.

By Bernouli's principle, faster flow speeds mean lower pressure

Hence the pressure differential causing lift



## Airfoils continued

U=airspeed  $\alpha$ =angle of attack c=chord  $\Gamma$ =circulation

- But why is the flow accelerated on the top surface?
- Because it must separate at the trailing edge.
- Therefore, aircraft can fly because of viscosity



(a) Flow with no circulation.



(b) Circulatory flow only.







Camber increases the amount of lift produced by the airfoil

Symmetric airfoil - no lift at 0° aoa









#### **Pressure distribution**

• The static pressure around a lifting airfoil looks something like:





## Lift

 The amount of lift produced by an airfoil is also proportional to the total circulation required for the flow to separate at the trailing edge

$$l = \rho U \Gamma$$

- Where  $\rho$  is the air density, U the free stream airspeed and  $\Gamma$  the circulation.
- For flat plates and small angles of attack this result simplifies to

 $l = \pi \rho U^2 \alpha$ 



#### Lift coefficient

 A lift coefficient is a non-dimensional quantity defined as

$$c_l = \frac{\iota}{\frac{1}{2}\rho U^2 c}$$

• For a flat plate, the lift coefficient can be obtained from

$$c_l = 2\pi\alpha$$



#### True lift

As shown in the video earlier the flow cannot remain attached to the wing's surface at high angles of attack.

Flow separation results in loss of lift. Important characteristics:

- Maximum lift coefficient
- Maximum lift angle of attack





- The lift is a single force but it is caused by a continuous pressure distribution.
- Therefore, it must have a point of application. This point is called the Centre of Pressure (cp).
- The moment caused by the lift acting at the cp around the leading edge is called the pitching moment.
- Pitching moment coefficient:

$$c_m = \frac{m}{\frac{1}{2}\rho U^2 c^2}$$



Drag

Unfortunately, all bodies in a real airflow are subjected to a drag force.

There are no easy expressions for the calculation of drag. There are many sources of drag and few of them are easily modeled.

Drag: d

Drag coefficient:

$$c_d = \frac{d}{\frac{1}{2}\rho U^2 c}$$





#### The boundary layer

- Drag in two dimensions cannot be modeled at all using inviscid assumptions
- Prandtl was the first to realize that viscous effects are very important in a thin layer of flow near the wing's surface
- Skin friction and momentum deficit within the boundary layer are some of the major sources of drag



#### Momentum deficit

• Momentum deficit can be visualized as:



• The flow in front of the airfoil and just after it looks like:



 In other words, momentum has been lost. Loss of momentum = drag force.



#### **Graphical representation**





Stall

TYPE I TRAILING EDGE STALL

TYPE & LEADING EDGE STALL



TYPE T THIN AIRFOIL STALL



a. Upper surface pressure distributions, growth of the boundary layer and separation regions and lift and pitching moment curves.



b. Stalling characteristics correlated with Reynolds number and airfoil geometry (Ref. 7-81)



#### Coordinate system

- The values of lift and drag also depend on the coordinate system we choose.
- The most consistent definition of lift and drag is:
  - Lift is a force perpendicular to the free stream.
  - Drag is a force parallel to the free stream.
- Therefore, the integral of the pressure distribution around the airfoil is not the lift but the force acting normal to the surface:

$$n = \int_0^c (p_l(x) - p_u(x)) dx$$

 So that the actual lift is *l=ncosα*. In general, if the normal, *n*, and tangential, *n*, forces are known:

$$l = n\cos\alpha - t\sin\alpha$$

$$d = t\cos\alpha + n\sin\alpha$$





#### Airfoil characteristics

**Design Parameters** 

- Chord length, (c)
- Thickness, (t)
- Camber, (dz/dx)
- Shape (e.g. NACA 0012)

#### **Performance Parameters**

- Lift curve slope ( $c_{l\alpha}$ )
- Zero-lift angle  $(c_{l0})$
- Maximum lift angle  $(\alpha_{clmax})$
- Maximum lift coefficient
  (c<sub>lmax</sub>)
- Minimum drag coefficient

$$(c_{d\min})$$



## NACA 4-digit Airfoils

- These airfoils were developed in the 20s and 30s based on earlier Göttingen and Clark Y sections
- They use a very specific terminology





## NACA 4-digit airfoils

- Defined by  $\pm y_{t} = \frac{t/c}{0.2} \left( 0.2969 \sqrt{x} - 0.1260 x - 0.3516 x^{2} + 0.2843 x^{3} - 0.1015 x^{4} \right)$   $y_{c} = \frac{c_{\max}/c}{p^{2}} \left( 2x_{c_{\max}} x - x^{2} \right) \quad \text{from } x = 0 \text{ to } x = x_{c_{\max}}$   $y_{c} = \frac{c_{\max}/c}{(1-p)^{2}} \left( \left( 1 - 2x_{c_{\max}} \right) + 2x_{c_{\max}} x - x^{2} \right) \quad \text{from } x = x_{c_{\max}} \text{ to } x = c$
- Where  $y_{upper} = y_t + y_c$ ,  $y_{lower} = -y_t + y_c$ ,  $y_t$  is the thickness shape and  $y_c$  is the camber shape,  $x_{cmax}$  is the chordwise position of maximum camber, t is the maximum thickness and  $c_{max}$  is the maximum camber.





 A wing can be seen as an extrusion of an airfoil in the ydirection.

Wing span: *b* 

Wing half-span: s=b/2

Wing area over full span: *S* 

Aspect ratio:  $AR=b^2/S$ 





#### Forces on wings

 In principle, it is simple to calculate the aerodynamic lift acting on a wing: it is simply the integral of the sectional lift over the span:

$$L = \int_{-s}^{s} l(y) dy, \text{ or, } C_{L} = \int_{-s}^{s} c_{l}(y) dy, \text{ where } C_{L} = \frac{L}{1/2\rho U^{2}S}$$

 Unfortunately, the sectional lift variation is not easy to calculate



#### 2D vs 3D force coefficients

- 2D lift, drag, moment etc. coefficients:
  - Use lowercase letters:  $c_l$ ,  $c_d$ ,  $c_m$ , etc.
  - Use chord or chord<sup>2</sup> to normalize, e.g.

$$c_d = \frac{d}{\frac{1}{2}\rho U^2 c}, \ c_m = \frac{m}{\frac{1}{2}\rho U^2 c^2}$$

- 3D lift, drag, moment etc. coefficients:
  - Use uppercase letters:  $C_L$ ,  $C_D$ ,  $C_M$ , etc.
  - Use surface area or surface\*chord to normalize, e.g.

$$C_D = \frac{D}{\frac{1}{2}\rho U^2 S}, \ C_M = \frac{M}{\frac{1}{2}\rho U^2 S c}$$



# Lifting line theory

The wing is modeled mathematically by a single horseshoeshaped vortex (black line)



showing that the horse-shoe vortex is a good approximation of real flow

The stronger the vortex, the higher the lift



 Tip vortices of large aircraft can cause serious problems in airports.

#### Wingtip vortex visualization

#### Milestones in Flight History Dryden Flight Research Center





#### Induced drag

- Three-dimensional wings feature one very clear and simple to quantify source of drag: induced drag.
- In essence, the fact that a wing produces lift means that it also produces drag.
- The drag is proportional to the square of the lift.
- The source of induced drag is a downwash flow velocity created on the wing by the trailing vortices.





#### Induced drag (2)



The lift acting on a 3D wing is not perpendicular to the free stream, it is perpendicular to the total airspeed due to the free stream and downwash. The lift component perpendicular to the free stream is approximately equal to *l* for small downwash angles.

The lift component parallel to the free stream is the induced drag, given by

$$d = l\varepsilon$$



 $C_l$ 

- It can be shown that a wing with an elliptical planform has an elliptical wing distribution
- Furthermore, this wing distribution causes the minimum liftinduced drag

For such a wing the total lift  $\mathcal{Y}$ and induced drag can be easily calculated:

$$C_L = \frac{2\pi AR}{AR + 2}\alpha \qquad \qquad C_D = \frac{C_L^2}{\pi AR}$$

Aspect ratio decreases  $C_D$ 



#### More on lift distributions

- Few well-known aircraft ever featured an elliptical wing.
- Minimizing lift-induced drag is only one consideration in the design of wings.
- Most wings have non-elliptical lift distributions.
- The lift and induced drag can be calculated for such wings using lifting line theory.







## Sources of drag

- Parasite drag:
  - Skin friction drag (friction)
  - Form drag (also known as pressure or profile drag)
  - Interference drag (vortices created at the intersection of surfaces)
- Induced drag (due to downwash of wings)
- Wave drag (supersonic drag)


# Wing characteristics

- Aspect Ratio
- Twist: angle of attack at root is not the same as angle of attack at tip
- Taper: chord at tip is smaller than chord at root
- Thickness ratio: Wing thickness varies over the span
- Airfoil: may change over wingspan
- Sweep: wingtip lies behind or in front of wing root



#### Aspect Ratio



Low aspect ratio wing F-15

# High aspect ratio wing B-52





#### Aspect Ratio

- The Aspect Ratio is one of the basic design parameters for transport aircraft.
- It has a significant effect on aircraft performance. This will be discussed at a later lecture.
- Large values of AR tend to make the flow around the wind more 2D.
- Remember that 2D flows do not cause induced drag.
- Therefore, a very high aspect ratio increases the lift coefficient and decreases the drag coefficient.



#### Twisted wings





# Wing twist

- Wash-in:  $\alpha_{tip} > \alpha_{root}$
- Wash-out:  $\alpha_{tip} < \alpha_{root}$



The effect of twist is usually modeled by defining the basic lift distribution (no twist) and the additional lift distribution (lift due only to twist)

Wings often have washout to reduce structural weight and improve stall characteristics



# More on wing twist

- The point of initial stalling should be sufficiently inboard, around 0.4*s* from the wing root.
- This can be achieved with suitable twist. If the stall point is too far outboard, a little washout will bring it inboard.
- However, a washout of more than 5° results in an unacceptable increase in induced drag.



# **Tapered Wings**

#### Most World War II fighter aircraft had tapered wings







# Wing taper

- The taper ratio is defined as  $\lambda = c_{tip} / c_{root}$
- Taper reduces the amount of lift produced near the wing-tip.
- Consequently, the tip vortex is weaker and the induced drag is decreased.
- Taper also reduces structural weight
- As the chord at the root is unchanged the maximum lift is not severely affected by taper
- If the taper is not too high, the stalling characteristics are acceptable, even without twist





### Non-linear taper

• Taper doesn't have to be linear

P-51 Mustang









#### No taper

 Untapered wings are easy and cheap to manufacture but aerodynamically inferior to tapered wings

Cessna 120









## Thickness-to-chord ratio

- High Aspect Ratio is good for transport aircraft: it decreases the induced drag coefficient.
- For such wings to be structurally sound, they must be very thick near the root.
- This is usually achieved by increasing the thickness ratio near the wing
- Thickness affects also the profile drag. Too much increase in thickness can cancel the decrease in induced drag due to high AR.



### Thickness-to-chord ratio

- Thickness ratio also affects
   the maximum lift
- Optimal thickness ratios:
  - 15-20% near the wing root
  - 10-15% near the wing tip
- Higher than 20% is not good





# Airfoil selection

- The airfoil section does not affect the wing lift distribution at small angles of attack
- It affects mainly:
  - The curve of local  $c_{lmax}$
  - The profile drag





# Airfoil choices

- NACA four-digit airfoils:
  - Drag increase with lift is gradual
  - Cambered sections have good maximum lift and docile stall
  - Gradual changes in drag and pitching moment
  - They are used in light aircraft (mostly wingtips and tailplanes) and trainers (gradual changes are good for training aircraft).
- NACA five-digit
  - Better maximum lift than 4-digit but very abrupt stall
  - They are sometimes used inboard, combined with 4-digit airfoils near the wingtip.



### More airfoils

- NACA 6-series
  - Also known as 'laminar flow' series
  - Designed to have low profile drag at low lift coefficients - the 'low drag bucket' region
  - They also have high critical Mach numbers
  - Lower maximum lift than 4- and 5-digit series
  - Extensively tested and very well documented



- In short, airfoil selection should be made using the following considerations:
  - An airfoil with low profile drag at the design flight conditions must be chosen
  - The airfoil must be capable of giving the desired maximum lift to the wing (with flaps if needed)

Compressibility issues must be addressed



- High subsonic cruise Mach numbers can be attained by:
  - Using sweepback
  - Reducing the thickness-to-chord ratio
  - Using improved airfoil sections
    - ('supercritical airfoils')
  - Optimizing spanwise camber and twist variation



### Zero sweep angle

- BAe ATP: Maximum airspeed of 137m/ s at 25000ft, i.e. maximum M=0.44
- Straight tapered wings





# High sweep angle

- Airbus A380: Maximum airspeed of 265m/s at 35000ft, i.e. maximum M=0.89
- Highly swept tapered wings





### Types of sweep



Straight quarter-line chord

Reduced sweep at inboard section

Increased sweep at inboard section



# Effect of sweep

A component of the free stream airspeed,  $V_{\rm T}$  is tangent to the wing. Therefore, the airspeed seen by the airfoil is only  $V_{\rm N}$ 

 $V_{\rm N} = V_{\infty} \cos \Lambda$ 

The effective Mach number seen by the wing's airfoil is

 $M_{\rm eff} = M_{\infty} \cos \Lambda$ 

A higher  $V_{\infty}$  is required to achieve the sonic conditions





# Using sweepback

- Up to *M*=0.65 or *M*=0.7, straight wings with appropriate thickness ratio are sufficient.
- At higher Mach numbers, sweepback is required
- A sweep angle of 35 degrees is rarely exceeded



# Sweep data

It is clear that sweep angle increases with Mach number.

Taper ratio also, generally, increases with Mach number.

Aircraft	Aspect Ratio	Taper Ratio	Sweep Angle	Maximum
				Mach
VFW-Fokker	7.22	0.402	15°	0.65
614				
Yakovlev Yak	9.00	0.396	$0^{\rm o}$	0.70
40				
Fokker-VFW F	7.27	0.355	16°	0.75
28				
BAC 1-11	8.00	0.321	20°	0.78
200/400				
Aerospatialle	8.02	0.354	$20^{\circ}$	0.81
Caravelle				
Boeing 737	8.83	0.251	25°	0.84
100/200				
MDD DC-8	7.30	0.244	30°	0.88
10/50/60				
Boeing 707	7.11	0.293	35°	0.90
Boeing 747	6.96	0.309	37°30'	0.92



### Shock waves

 Shock waves can be formed on the upper (and even lower) surfaces of wings travelling in transonic (i.e. M<1) flow. For example:





# Airfoils for Transonic Conditions



a. Conventional section
 with roof-top pressure
 distribution

b. Peaky upper surface pressure distribution



c. Supercritical upper surface pressure distribution d. Rear loading airfoilcompared with conventionalairfoil (lower surface)



### Transonic airfoils

- Rooftop: They have a relatively flat pressure distribution on the forward upper surface. The flow is not accelerated in this region and the advent of M=1 is delayed. NACA 6-series
- Peaky upper surface: Supersonic velocities and suction near the leading edge, followed by a weak shock wave. The drag rise is postponed to higher airspeeds. BAC 1-11, VC-10 and DC-9 have used this.



# Transonic airfoils

- Supercritical airfoils: They have a flat upper surface, creating shock-free supersonic flow region. This region is much greater than that of the peaky distribution
- Rear loading: The rear lower surface is highly cambered so that a lot of lift is generated near the rear of the airfoil. When combined with a flat upper surface (supercritical airfoil) a large decrease in drag for the same Mach number and lift coefficient can be obtained.
- This combination has been used by Airbus A300 and all subsequent civil transports



 A value for the most appropriate thickness ratio for a particular Mach number can be obtained from

$$t / c = 0.3 \left\{ \left[ 1 - \left( \frac{5 + M^2}{5 + M^{*2}} \right)^{3.5} \right] \frac{\sqrt{1 - M^2}}{M^2} \right\}^{2/3}$$

- Where  $M^*=1$  for conventional airfoils,  $M^*=1.05$  for peaky airfoils and  $M^*=1.15$  for supercritical airfoils
- *M*cos*A* can be used for sweptback wings



# Wing lift coefficient (unswept wings)

• The lift wing coefficient can be estimated by

$$C_{L} = C_{L_{\alpha}} \alpha$$

$$C_{L_{\alpha}} = 0.995 \frac{C_{l_{\alpha}}}{E + c_{l_{\alpha}} / \pi AR}$$

$$E = 1 + \frac{2\lambda}{AR(1 + \lambda)}$$

 $C_{L\alpha}$ =wing lift curve slope  $c_{l\alpha}$ =sectional lift curve slope E=Jone's correction  $\lambda$ =taper ratio AR=Aspect ratio



# Wing lift coefficient (unswept wings)

• For a sectional lift curve slope of  $2\pi$ 

$$C_{L_{\alpha}} = \frac{2\pi}{1 + \frac{2}{AR} \frac{1 + 2\lambda}{1 + \lambda}}$$

• Compressibility effects can be taken into account by replacing AR by  $\beta AR$ and  $C_{L\alpha}$  by  $\beta C_{L\alpha}$ , where

$$\beta = \sqrt{1 - M^2}$$



# Wing lift coefficient (swept wings)

• For swept wings, an approximate expression for the wing lift curve slope

is 
$$\beta C_{L_{\alpha}} = \frac{2\pi}{\frac{2}{\beta A R} + \sqrt{\frac{1}{k^2 \cos^2 \Lambda_{\beta}} + \left(\frac{2}{\beta A}\right)^2}}$$
where  $\tan \Lambda_{\beta} = \frac{\tan \Lambda_{1/2}}{\beta}$  and  $k = \frac{\beta c_{L_{\alpha}}}{2\pi}$ 
 $\Lambda_{1/2}$  is the sweepback angle at the half-

chord



• The maximum lift coefficient of a wing can be approximated by

$$C_{L_{\max}} = k_s \frac{c_{l_{\max, root}} + c_{l_{\max, tip}}}{2}$$

• Where  $k_s = 0.88$  for untapered wings and  $k_s = 0.95$  for tapered wings.



### Wing-fuselage interference

The fuselage produces very little (if any) lift. However, some lift is carried over from the wing onto the fuselage.



Fig. E-11. Fuselage/wing interference effects on the spanwise lift distribution.



# Supersonic flight

- Supersonic flight requires different wing design because:
  - Lift generation mechanisms are different
  - Much more drag is produced
- Supersonic airfoils are usually very thin and sharp
- Supersonic wings are either trapezoidal or Delta-shaped



### Trapezoidal wings

#### Bell X-1




Delta Wings Concorde



MiG-21

Mirage 2000







#### Supersonic flow over flat plate



 $p_{\boldsymbol{u}}$  is lower than  $p_{\boldsymbol{l}}$  so that there is a net force upwards - lift



## Lift on supersonic flat plate

- It is easy to calculate the lift on a flat plate airfoil in a supersonic flow
- The compression and expansion cause
   pressure coefficients of

$$c_{p_l} = \frac{2\alpha}{\sqrt{M^2 - 1}}$$
  $c_{p_u} = -\frac{2\alpha}{\sqrt{M^2 - 1}}$ 

- The force acting normal to the plate is  $c_n = \frac{1}{c} \oint c_p dx = \frac{1}{c} \int_0^c (c_{p_l} - c_{p_u}) dx = \frac{4\alpha}{\sqrt{M^2 - 1}}$
- Leading to a lift coefficient of:

$$c_l = c_n \cos \alpha = \frac{4\alpha}{\sqrt{M^2 - 1}}$$



- Unlike incompressible flow, supersonic flow causes drag, known as wave drag.
- The drag force is obtained from the normal force as

$$c_d = c_n \sin \alpha = \frac{4\alpha^2}{\sqrt{M^2 - 1}}$$



The difference in shock strengths causes the flow on the lower surface to be compressed more than the flow on the upper surface.



## **Delta Wing**

- Lift is generated on a Delta wing by the creation of conical vortices
- High speed flow under the vortices causes low pressure
- Pressure difference with lower surface causes lift





## Lift on Delta Wing

Lift contribution from potential and vortex

$$C_{L} = C_{L,P} + C_{L,V} =$$

$$K_{P} \sin \alpha \cos^{2} \alpha + K_{V} \cos \alpha \sin^{2} \alpha$$
Where  $\alpha$  is the angle of attack  
and  $K_{P}$ ,  $K_{V}$  come from the  
drawing





#### Vortex burst

- At very high angles of attack the vortices can break down
- Loss of lift ensues





## Delta Wings at low speeds

- Delta wings are quite inefficient at low speeds
- Concorde had to fly at an uncomfortably high angle of attack to take off and land
- Several solutions have been tried
  - Canards
  - Compound Delta
  - Swing-wing
  - Leading Edge Extensions



### Canards

 This was the solution adopted by the Tu-144

The canards were there specifically to control the aircraft at low airspeeds





#### **Compound Delta**

#### Saab-35 Draken

Two Delta wings superimposed, with different sweeps. The highly swept section creates additional, stronger vortices that increase lift and serve to keep the flow attached at higher angles of attack

F-16XL





# Swing-Wing

 Quite a simple concept: at high speeds you get a Delta, at low speeds you get a high AR trapezoidal wing







- Some aircraft combine the advantages of Delta wings with those of trapezoidal wings
- Leading Edge Extensions (as on this F-18) create vortices just as Delta Wings
- The vortices can keep the flow over the wing attached at very high angles of attack

